

1.  $7^\circ 12'$ : 8 grades.      2.  $\frac{4\pi}{15}$ ,  $\frac{\pi}{3}$ ,  $\frac{2\pi}{5}$ .      4.  $\frac{3}{2}$ .  
 5.  $15\sqrt{3}=25.98$  m.      6. 790 m.      7. 1.745 m.  
 8.  $\frac{8}{17}$ ,  $\frac{15}{17}$       9.  $30^\circ, 60^\circ$ .      10.  $\frac{125}{78}$ .      12.  $\frac{1-\tan^2 A}{\tan^4 A}$ .  
 17. (1)  $45^\circ$ ; (2)  $60^\circ$ .      18. 327.2 m.      21. 200, 183 nearly.  
 22. .09375; 16.7552.      24.  $\sqrt{2} : 1$ .      25. 1;  $\tan A$ .  
 27.  $-\frac{5}{31}$ .      28.  $45^\circ$  or  $60^\circ$ .      29.  $15^\circ 12' 45''$ .  
 30. 260.26 m.      32. (1)  $60^\circ$ ; (2)  $60^\circ$ .      33.  $6^\circ 18'$ .  
 34. sine =  $\frac{24}{25}$ , cosine =  $\frac{7}{25}$ , tangent =  $\frac{24}{7}$ .  
 35. (1) and (3) are impossible, (2) and (4) possible.  
 37.  $B=45^\circ$ ,  $b=25\sqrt{2}$ ,  $p=25$ .      39.  $-\frac{\sqrt{3}}{2}$ ,  $-2$ ,  $\frac{1}{\sqrt{3}}$ .  
 40.  $45^\circ, 135^\circ, 225^\circ, 315^\circ, 405^\circ, 495^\circ$ .      42.  $15^\circ, 75^\circ$ .  
 45.  $30^\circ, 150^\circ, 270^\circ$ .      46.  $\pm 8$ .      47.  $\frac{16}{65}$ .  
 48.  $\tan 2A$ .      49.  $\pm \frac{1}{\sqrt{3}}$ .      50.  $500(3+\sqrt{3})=2366$  m.  
 51. (1) 0; (2)  $-2$ .      53.  $\frac{a^2-b^2}{a^2+b^2}$ .      55.  $-\sqrt{3}$ ,  $-\frac{1}{2}$ ,  $\frac{1}{\sqrt{3}}$ .  
 56.  $6\frac{4}{11}^\circ$ .      57.  $-\frac{15}{352}$ .      59. (1)  $\cot C$ ; (2) 2.  
 60.  $50\sqrt{6}$  m.      66.  $50\sqrt{3}=86.6$  m.      67. 3.141.  
 70.  $-1$ .      73.  $\frac{1}{2} \sin 2\theta$ .      74.  $x^{\frac{2}{3}}+y^{\frac{2}{3}}=4^{\frac{2}{3}}$ .  
 75.  $5\sqrt{3}$  m.;  $5(3+\sqrt{3})$  m.;  $20+5\sqrt{3}$  m.      77. 22.5 cm.  
 84. 4.14 km.      89. .38021, 3.73239, 9.76143.  
 95.  $27^\circ 45' 44''$ .      97.  $\sin 2A = -\frac{336}{625}$ ;  $\tan \frac{A}{2} = -\frac{1}{7}$ .  
 98.  $2-\sqrt{3}$ .      99.  $\bar{2}.60206, 1.3802113, \bar{1}.8239087$ .  
 102. 45, 53;  $58^\circ 6' 33.2''$ .      104.  $120^\circ$ .      106.  $\frac{20}{21}$ .  
 107.  $4 \operatorname{cosec} 2\theta$ .      108.  $49^\circ 28' 32''$ .  
 110. 2.30103,  $\bar{2}.39794$ , .598626, 9.69897, 9.849485.  
 112. 114 yds., 57 yds.      114.  $53^\circ 7' 48''$ .      115. .8, 1.25.

116. .90309, 1.10739,  $\bar{8}$ .52575.      117.  $\frac{1}{\sqrt{2}}$ .  
 118.  $-\tan \frac{\alpha}{2} \cot \frac{\beta}{2}, \tan \frac{\alpha}{2} \tan \frac{\beta}{2}$ .      120. 13.5 m;  $58^{\circ}6'$ .  
 122. 1.60206,  $\bar{1}$ .562469.      123.  $34^{\circ}18'1''$ ,  $1^{\circ}41'59''$ .  
 127.  $\pm \frac{2\sqrt{5}}{5}$ .      131. 1.3011928.  
 137. .69897, .845098, 1.113943.  
 138.  $49^{\circ}19'30''$ ,  $40^{\circ}40'30''$ .      143. .4855934.  
 144.  $39^{\circ}35'11''$ ,  $28^{\circ}20'49''$ .  
 146. 2.0755469, .3853509,  $\bar{1}$ .9256038.  
 149.  $100\sqrt{2}$ ,  $50\sqrt{2}$ ;  $71^{\circ}33'54''$ ,  $108^{\circ}26'6''$ .  
 150.  $\operatorname{cosec} x - \operatorname{cosec} 3x$ .      152.  $45^{\circ}$ ,  $60^{\circ}$ ,  $120^{\circ}$ ,  $135^{\circ}$ .  
 154.  $-\frac{56}{33}$ ;  $\frac{4}{5}$ ;  $\frac{12}{13}$ ;  $-\frac{33}{65}$ ;  $120^{\circ}30'37''$ .  
 158. .30103, .477121, 1.041393.      160.  $68^{\circ}52'42''$ .  
 161.  $\frac{\text{area of circle}}{\text{area of octagon}} = \frac{1380}{1309}$ .      165.  $\frac{c \sin \beta}{\sin(\alpha+\beta)}, \frac{c \sin \alpha \sin \beta}{\sin(\alpha+\beta)}$   
 166.  $-4 \cos \frac{\alpha}{2} \cos \frac{\beta}{2} \cos \frac{\gamma}{2}$ .      173.  $B=4^{\circ}55'11''$ ,  $C=178^{\circ}27'25''$ .  
 176.  $B=105^{\circ}$ ,  $C=45^{\circ}$ ,  $a=\sqrt{2}$ .  
 178.  $B=81^{\circ}47'12''$  or  $98^{\circ}12'48''$ ;  $c=13$  or  $11$ ;  
 $C=68^{\circ}12'48''$  or  $51^{\circ}47'12''$ .  
 180. 3333.3 m.      186.  $64^{\circ}31'58''$ .  
 191. 2310 sq m; 55 m, 66 m, 70 m.  
 193. (1)  $n\pi, \frac{n\pi}{2} \pm \frac{\pi}{16}$ ; (2)  $n\pi \pm \frac{\pi}{6}$ .  
 197. 134.19 m.      204. 226.87.      206.  $\frac{4}{3}, -\frac{3}{8}$ .  
 212. (1)  $(2n+1)\frac{\pi}{8}, n\pi + (-1)^n \frac{\pi}{4}$ ; (2)  $n\pi, n\pi + \frac{3\pi}{4}$ .  
 214. 10 m.      219.  $\frac{1}{4}$  or  $-8$ .      222. 37.27919 m.  
 231.  $4\frac{1}{2}$  km approximately.      233.  $\pm \frac{7}{23}$ .

235. (1)  $\frac{n\pi}{4}, \frac{2n\pi}{3} \pm \frac{\pi}{9}$ ; (2)  $n\pi + \frac{\pi}{3}, n\pi + \frac{3\pi}{4}$ .

242.  $10^\circ$ .

246. 205.4.

252. 1224.35 m.

256. 9.65146, 20.5309.

262.  $\alpha + \beta + \gamma = (2n + 1) \frac{\pi}{2}$ .

264.  $\sqrt{2}$  km.

266.  $\theta = n\pi$ .

275.  $B = 70^\circ 0' 57''$  or  $109^\circ 59' 3''$ ;

$C = 59^\circ 59' 3''$  or  $20^\circ 0' 57''$ . 277.  $\theta$ .

279.  $\cos(\alpha + \beta + \gamma + \delta) + \cos(\alpha + \beta - \gamma - \delta) + \cos(\alpha + \gamma - \beta - \delta)$   
 $+ \cos(\alpha + \delta - \beta - \gamma)$ .

281. 4.

283.  $A = 45^\circ, B = 112\frac{1}{2}^\circ, c = \sqrt{2 - \sqrt{2}}$ .